1-3 Properties of Numbers

Evaluate each expression if a = -1, b = 4, and c = 6. 31. 4a + 9b - 2cSOLUTION: 4a + 9b - 2c = 4(-1) + 9(4) - 2(6)= -4 + 36 - 12= 32 - 12= 2032. -10c + 3a + aSOLUTION: -10c + 3a + a = -10(6) + 3(-1) + (-1)= -60 + (-3) + (-1)= -63 + (-1)= -6433. a - b + 5a - 2bSOLUTION: a-b+5a-2b = (-1)-4+5(-1)-2(4)= -1 - 4 + (-5) - 8=(-1-4)+(-5-8)= -5 + (-13)= -1834. 8a + 5b - 11a - 7bSOLUTION: 8a + 5b - 11a - 7b = 8(-1) + 5(4) - 11(-1) - 7(4)= -8 + 20 + 11 - 28=(-8+20)+(11-28)=12 + (-17)= -5 $35.3c^2 + 2c + 2c^2$ SOLUTION: $3c^{2} + 2c + 2c^{2} = 3(6^{2}) + 2(6) + 2(6^{2})$ = 3(36) + 2(6) + 2(36)=108+12+72

$$= (108 + 12) + 72$$
$$= 120 + 72$$
$$= 192$$

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36. 3a - 4a^2 + 2a

SOLUTION:

3a - 4a^2 + 2a = 3(-1) - 4(-1)^2 + 2(-1)

= -3 - 4(1) - 2

= -3 - 4 - 2

= (-3 - 4) - 2

= -7 - 2

= -9
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55. JUSTIFY ARGUMENTS Explain why 0 has no multiplicative inverse.

SOLUTION:

0 has no multiplicative inverse. You cannot divide by 0.

57. **JUSTIFY ARGUMENTS** Does the Commutative Property *sometimes, always* or *never* hold for subtraction? Explain your reasoning.

SOLUTION:

Sometimes; when a number is subtracted by itself then it holds but otherwise it does not.

58. **ANALYZE RELATIONSHIPS** Explain whether 1 can be an additive identity. Give an example to justify your answer.

SOLUTION:

1 cannot be an additive identity. $3 + 1 \neq 3$

59. WHICH ONE DOESN'T BELONG? Identify the equation that does not belong with the other three. Explain your reasoning.



SOLUTION:

(2j)k = 2(jk); The other three equations illustrate the Commutative Property of Addition or Multiplication. This equation represents the Associative Property of Multiplication.

1-3 Properties of Numbers

61. Abassi will use the Additive Identity Property to solve an equation. Which of the following best illustrates the Additive Identity Property?

A $a \cdot 1 = a$ **B** b + 0 = b **C** c + (-c) = 0**D** d + 1 = d + 1

SOLUTION:

The Additive Identity Property states that the sum of any number and 0 is that number. b + 0 = b means that a number *b* plus 0 is equal to *b*. This is an illustration of the Additive Identity Property.

So, choice B is the correct answer.

62. When a number is tripled, its value increases by 10. What is the original number?

F 5 **G** 10 **H** 15 **J** 30

SOLUTION:

"When a number is tripled" means that a number is multiplied by 3. Let n represent that number and 3n represent the number multiplied by 3.

"Its value increases by 10" means to add 10 to the number. So, n + 10 represents the sum of the number and 10.

Set the expressions equal to each other and solve for n.

 $3n = n + 10 \quad \text{Original equation} \\ 2n = 10 \quad \text{Subtract } n \text{ from each side.} \\ n = 5 \quad \text{Divide each side by 2.}$

So, the original number is 5 and the correct answer is choice F.

63. Which property justifies rewriting the equation $\frac{1}{6} \cdot 6 + z = 8$ as 1 + z = 8?

A Additive Identity Property

- B Multiplicative Identity Property
- C Multiplicative Inverse Property

D Substitution

SOLUTION:

The Multiplicative Inverse Property says that $\frac{a}{b} \cdot \frac{b}{a} = 1$.

Substitute 1 for *a* and 6 for *b* to get $\frac{1}{6} \cdot \frac{6}{1} = 1$.

This is the property demonstrated in the equation, so the correct answer is choice C.

1-3 Properties of Numbers

64. A company creates mobile apps for a smartphone. When the app was free, they had 880 downloads. After the price was set to \$0.99, they had *d* downloads. The company receives \$0.70 in revenue for each app that is sold for \$0.99. Which equation gives the average revenue *R* for all downloads of this app?

$$F R = \frac{0.7d}{880 + d}$$

$$G R = 0.7(880 - d)$$

$$H R = 0.7d$$

$$J R = \frac{0.7}{880 + d}$$

SOLUTION:

The average revenue is equal to the total revenue divided by the total number of downloads.

Let *R* represent the average revenue and *d* represent the number of downloads when the app was \$0.99.

To find the total revenue add the revenue from when the app was free to the revenue from when the app was 0.99. When the app was free, the revenue was 0.99. Now that the app is 0.99, the revenue is 0.70 per app. So 0.7d represents the amount of revenue from when the app was 0.99. Since there was no revenue when the app is free, this is also the total revenue.

To find the total number of downloads add the free downloads and the \$0.99 downloads. There were 880 downloads when the app was free and *d* downloads when the app was \$0.99, so the total number of downloads is 880 + d.

Therefore, $R = \frac{0.7d}{880+d}$ represents the average revenue. The correct answer is choice F.